$$\log_{a} b = x \Leftrightarrow a^{x} = b$$

$$\log_{e} b = x \Leftrightarrow e^{x} = b$$

$$\ln b = x \Leftrightarrow e^{x} = b$$

$$\log_2 32 = x$$

$$2^x = 32$$

$$x = 5$$

$$\log_{10} x = 3$$

$$\log x = 3$$

$$10^{3} = x$$

$$x = 1000$$

$$ln 1 = x$$

$$log_e 1 = x$$

$$e^x = 1$$

$$x = 0$$

$$\log_5 \frac{1}{125} = x$$

$$5^x = \frac{1}{125}$$

$$5^x = \frac{1}{5^3}$$

$$x = -3$$

$$\log_{8} \frac{1}{4} = x$$

$$8^{x} = \frac{1}{4}$$

$$8^{x} = \frac{1}{2^{2}}$$

$$8^{x} = 2^{-2}$$

$$(2^{3})^{x} = 2^{-2}$$

$$x = -\frac{2}{3}$$

